### IV Year II Semester 17EE837

## ADVANCED CONTROL SYSTEMS (Professional Elective-IV)

#### **Preamble:**

This subject aims to study state space, describing function, phase plane and stability analysis including controllability and observability. It also deals with modern control and optimal control systems.

### Learning objectives:

- 1. Review of the state space representation of a control system: Formulation of different models from the signal flow graph, diagonalization.
- 2. To introduce the concept of controllability and observability. Design by pole placement technique.
- 3. Analysis of a nonlinear system using Describing function approach and Phase plane analysis.
- 4. The Lypanov's method of stability analysis of a system.
- 5. Formulation of Euler Lagrange equation for the optimization of typical functional and solutions.
- 6. Formulation of linear quadratic optimal regulator (LQR) problem by parameter adjustment and solving riccatti equation.

#### Unit – I

State space analysis: State Space Representation – Solution of state equation – State transition matrix, –Canonical forms – Controllable canonical form – Observable canonical form, Jordan Canonical Form.

#### Unit – II

Controllability, observability and design of pole placement: Tests for controllability and observability for continuous time systems – Time varying case – Minimum energy control – Time invariant case – Principle of duality Controllability and observability form Jordan canonical form and other canonical forms – Effect of state feedback on controllability and observability – Design of state feedback control through pole placement.

## Unit – III

Describing function analysis: Introduction to nonlinear systems, Types of nonlinearities, describing functions, Introduction to phase-plane analysis.

#### Unit – IV

Stability analysis: Stability in the sense of Lyapunov – Lyapunov's stability and Lypanov's instability theorems – Direct method of Lypanov for the linear and nonlinear continuous time autonomous systems.

#### Unit – V

Calculus of variations: Minimization of functional of single function – Constrained minimization – Minimum principle – Control variable inequality constraints – Control and state variable inequality constraints – Euler lagrangine equation.

# Unit – VI

Optimal control: Linear quadratic optimal regulator (LQR) problem formulation – Optimal regulator design by parameter adjustment (Lyapunov method) – Optimal regulator design by continuous time algebraic riccatti equation (CARE) – Optimal controller design using LQG framework.

## **Learning Outcomes**

- 1. State space representation of control system and formulation of different state models are reviewed.
- 2. Able to design of control system using the pole placement technique is given after introducing the concept of controllability and observability.
- 3. Able to analyse of nonlinear system using the describing function technique and phase plane analysis.
- 4. Able to analyse the stability analysis using lypnov method.
- 5. Minimization of functional using calculus of variation studied.
- 6. Able to formulate and solve the LQR problem and riccatti equation.

# Text books:

- 1. Modern Control Engineering by K. Ogata, Prentice Hall of India, 3rd edition, 1998
- 2. Automatic Control Systems by B.C. Kuo, Prentice Hall Publication

## **Reference books:**

- 1. Modern Control System Theory by M. Gopal, New Age International Publishers, 2nd edition, 1996
- 2. Control Systems Engineering by I.J. Nagarath and M.Gopal, New Age International (P) Ltd.
- 3. Digital Control and State Variable Methods by M. Gopal, Tata Mc Graw– Hill Companies, 1997.
- 4. Systems and Control by Stainslaw H. Zak, Oxford Press, 2003. Optimal control theory: an Introduction by Donald E.Kirk by Dover publications.